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ON THE RAND: DETERMINANTS OF THE SOUTH AFRICAN EXCHANGE RATE

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**Abstract**
This paper is an econometric investigation of the determinants of the real value of the South African rand over the period 1984-2007. The results show a relatively good fit. As always with exchange rate equations, there is substantial weight on the lagged exchange rate, which can be attributed to a momentum component. Nevertheless, economic fundamentals are significant and important. This is especially true of an index of the real prices of South African mineral commodities, which even drives out real income as a significant determinant. An implication is that the 2003-2006 real appreciation of the rand can be attributed to the Dutch Disease. In other respects, the rand behaves like currencies of industrialized countries with well-developed financial markets. In particular, high South African interest rates raise international demand for the rand and lead to real appreciation, controlling also for a forward-looking measure of expected inflation and a measure of default risk or country risk.

JEL code: F31

Key words: South Africa, rand, commodity currency, Dutch Disease, mineral prices, country risk.

The rand has undergone large movements in recent years. What explains these swings?

Important questions include:

- Is the rand a commodity currency, like the Australian and Canadian dollar are said to be (to pick two floaters)? That is, is it a currency that appreciates when prices of the mineral products that it produces are strong on world markets and depreciates when they are weak?

- In other respects, does the rand behave like currencies of industrialized countries, in light of its developed financial markets? (South Africa borrows in rand, for example, unlike most developing countries.) This does not necessarily require that the exchange rate fit standard theories closely, as those theories don’t work well in practice for major industrialized currencies either. But such variables as GDP and rates of return should have an effect.

- Did the removal of capital controls in 1995, or other elements of the transition to

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This work was done with the able research assistance of Melesse Tashu. It is a contribution within the Macroeconomics Group of the Harvard University Center for International Development’s Project on South Africa: Performance and Prospects.
Relative to an earlier draft in mid-2006, the major innovations in this paper include: the addition of an absent theoretical model, the use of sovereign spread data to measure the risk premium and forward-looking inflation forecasts to measure real interest rates, allowing a break in 1995 for the end of apartheid and capital controls, and a dynamic simulation of the real value of the rand over 2003-2006. Thanks to Lesetja Kganyago, Ben Smit and other participants in the July 2006 meetings in Pretoria and to Brian Kahn, Stan du Plessis and other participants in the January 2007 meetings in Pretoria and Stellenbosch. None are implicated in the conclusions.
democracy, cause a structural break in the determinants of the real exchange rate?

- Has there been an element of momentum to some recent movements, or can they be explained by fundamentals?

Fig. 1 suggests that there has been a relationship between the real mineral price and real exchange rate: the currency slumps when mineral exports are declining, as in the late 1990s, but appreciates in natural resource booms as in 2002-2006 - the classic Dutch Disease. But Fig. 2 shows that the real exchange rate has the same correlation with relative real output, which could be explained either as a reflection of the Balassa-Samuelson effect (wherein productivity growth increases the price of nontraded goods relative to traded goods) or as a reflection of monetary theories of the nominal exchange rate (wherein growth in real income raises the demand for money and appreciates the currency nominally). We may have some trouble distinguishing the effect of mineral prices from the effect of real output, because the two are themselves highly correlated, as Fig. 3 shows.

**Figure 1. Real Exchange rate index(value of rand) and real mineral price index**

![Graph showing relationship between real exchange rate and real mineral price]
1. THEORETICAL BASIS OF MODEL

Here we focus on the determination of the real exchange rate, while recognizing that monetary factors are important. Our model of the real exchange rate divides its determinants into two categories, determinants of the long-run equilibrium exchange rate, and deviations of the current real exchange rate from its long-run equilibrium.

The long run equilibrium real exchange rate is given by a version of PPP:
\[
\bar{Q} \equiv \frac{SP^*}{P}, \quad \text{or in log form:} \quad q = s + p^* - p. \tag{1}
\]

where \(s \equiv \log\) of the nominal spot exchange rate, in rand per dollars.
\(p \equiv \log\) of the South African price level (probably a PPI or the GDP deflator)
\(p^* \equiv \log\) of the foreign (here US) price level.

But we define the price indices at home and abroad as Cobb Douglas functions of traded goods TG and non-traded goods NTG:
\[
p = \alpha p_{NTGSA} + (1-\alpha) p_{TGSA}, \tag{2}
\]
where \(\alpha\) is the weight placed on NonTraded Goods in the basket.
For simplicity we assume the same weights in the foreign country.

\[
p^* = \alpha p_{NTGSA} + (1-\alpha) p_{TGSA}, \tag{3}
\]

Combining (1), (2) and (3),
\[
q = s + p^* - p = s + [\alpha p_{NTGUS} + (1-\alpha) p_{TGUS}] - [\alpha p_{NTGSA} + (1-\alpha) p_{TGSA}].
= (s + p_{TGUS} - p_{TGSA}) + \alpha [(p_{NTGUS} - p_{TGUS}) - (p_{NTGSA} - p_{TGSA})]. \tag{4}
\]

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As Aron, Elbadawi and Kahn (2000). Chinn (1999) estimated a monetary model of the nominal rand exchange rate. Results for both the nominal and real rates were reported in Frankel (2006), an earlier version of the present paper.
The first term, \((s + p_{TGUS} - p_{TGSA})\), can be interpreted as the terms of trade, the relative price of the traded goods produced in the foreign basket in terms of traded goods produced at home. Our measure is the real price of the basket of six mineral commodities that South Africa’s most important exports, \(r m p\) in log form. Among those who have found mineral prices or the terms of trade to be an important determinant of the value of the rand are Aron, Elbadawi, and Kahn (2000), MacDonald and Ricci (2004), Mtonga (2006), Ngandu (2005), Ricci (2005), and Stokke (2006).

The second term is the relative price of nontraded goods in terms of traded goods, abroad versus at home, with weight \(\alpha\). Real appreciation occurs when the relative price of nontraded goods rises more rapidly in the domestic country than in the former country. According to the well-known Balassa-Samuelson relationship, this in turn happens when the rate of growth in productivity and income per capita is higher at home than abroad (because the productivity growth tends to be concentrated in the traded goods sector, where prices are tied to world prices by arbitrage).

Thus \((p_{NTGUS} - p_{TGUS}) = \beta(\text{income per cap})_{US}\) and \((p_{NTGSA} - p_{TGSA}) = \beta(\text{income per cap})_{SA}\).

Thus \(q_t = \mu r m p_t + \alpha \beta [(\text{income per cap})_{US} - (\text{income per cap})_{SA}]_t\). (5)

We have included both variables, the real price of South African minerals and relative income per capita, in the regression equation.

We turn now to the substantial short-term deviations, \((q - q\grave{} )\), that real exchange rates experience relative to their long-run equilibrium value \((q\grave{} )\). The idea is that such deviations arise routinely, but that they can be expected to correct themselves gradually over time, for example as sticky goods prices adjust. Assume that speculators form expectations according to the regressive specification, with the addition of a possible bubble component:

\[
E_t \Delta q = -\theta (q_t - q\grave{} ) + \delta q_{t-1}
\]

\[
E_t \Delta s = -\theta (q_t - q\grave{} ) + E_t \Delta p - E_t \Delta p^* + \delta q_{t-1}
\]

where \(E_t \Delta q\) is defined to be the expectation formed at time \(t\) of real depreciation over the coming period, and analogously for nominal depreciation and inflation; \(\theta\) is the expected speed of regression toward the long run equilibrium, the speed with which deviations are thought to be corrected; and \(\delta q_t\) is the possible bubble component.\(^2\)

\(^2\) Regressive expectations is of course the formulation in the classic Dornbusch (1976) overshooting model, in which this functional form for expectations is shown to be rational for the right value of \(\theta\) as a result of gradual adjustment of \(p\). Frankel and Froot (1987) offered evidence from survey data that expectations at the one-year horizon do indeed encompass such regressive behavior. Rationales for the addition of the term \(\delta q_t\) go back to the bubble literature of the late 1980s, e.g., the “dragging anchor” in Goodhart (1985) or the “overshooting of the overshooting equilibrium” in Frankel and Froot (1990). Some think that bandwagons or bubbles may have affected the rand at some points (e.g., the sharp fall in 2002). In any case, whatever the rationale, many studies, of which Mark (1995) is perhaps the best-known, have found empirically that an equation that includes the lagged exchange rate together with current fundamentals performs better than either fundamentals alone or the lagged rate alone (random walk), especially at longer
Assume also that uncovered interest parity holds, except for the country premium (default risk premium) that drives a wedge between South African interest rates and foreign interest rates, as reflected in the sovereign spread.

\[ E_t \Delta s = (i_{SA t} - i_{SA* t}) - (risk \ spread) \]  

(7)

Now we combine equations (6) and (7) -

\[ \theta (q_t - \bar{q}) + E_t \Delta p - E_t \Delta p^* + \delta q_{t+1} = (i_{SA t} - i_{SA* t}) - (risk \ spread) \]

and solve for the current real exchange rate:

\[ q_t = \frac{-1}{\theta} \left[ \frac{1}{\theta} \left( i_{SA t} - i_{US* t} \right) - (E_t \Delta p - E_t \Delta p^*) \right] + \frac{1}{\theta} (risk \ spread) \]  

(8)

Now bring this half of the model together with the other half, equation (5):

\[ q_t = \frac{\delta}{\theta} q_{t+1} + \mu \cdot \text{rmp}_t - a_1 \beta \left[ \text{income pc}_{SA} - \text{income pc}_{US} \right] - \frac{1}{\theta} \left( r_{SA} - r_{US} \right) + \frac{1}{\theta} (risk \ spread) \]  

(9)

where we have defined the domestic and foreign real interest rates:

\[ r_{SA t} = i_{SA t} - E_t \Delta p \]  

and \[ r_{US t} = i_{US t} - E_t \Delta p \]  

Equation (9) represents our model.

2. ESTIMATED EQUATION

As we turn to the empirical estimation, we begin to work in terms of the real value of the rand, rather than its reciprocal the real exchange rate, in order to maximize the user-friendliness of the coefficient signs and graphs. Our general equation is:

Log Real Value of Rand, \( t = \)

\[ \alpha + \beta_1 \text{ Log Real Rand Value }_{t-1} + \beta_2 \text{ Log Real World Mineral Price }_{t} + \beta_3 \text{ Log (SA GDP per cap/foreign GDP per cap) }_{t} + \beta_4 \text{ Real Interest Differential }_{t} + \beta_5 \text{ Country Risk Spread }_{t} + \beta_6 \text{ trend }_{t} + \beta_7 \text{ CapLib }_{t} + \beta_8 \text{ CapLib*RID }_{t} + \beta_9 \text{ u }_{t}. \]

- We have tried various versions of the equation: with the value of the rand defined bilateral against the dollar, or trade weighted.
- \text{Log Real Rand Value }_{t-1} \text{ is entered to capture the idea of a dragging anchor or momentum elements. Hypothesis: } 0 < \beta_1 < 1.
- Real World Mineral Price, \text{ is computed as an appropriately weighted average of the prices of the specific mineral products that South Africa produces and exports. It is intended to capture the terms of trade, and so is expressed in real form by deflating by the foreign price level. Hypothesis: } \beta_2 > 0.
- (SA GDP per cap/foreign GDP per cap) , often appears in nominal exchange rate equations as an important determinant of the demand for money (domestic relative to foreign). We are on firmer ground theoretically, when seeking to explain the real exchange rate, to invoke a Balassa-Samuelson effect, in which case real output \text{ per capita is the more relevant variable. In any case, it is only possible to include the GDP variable when we are working with quarterly data; we are forced to drop it when working with monthly data, unless we interpolate. Hypothesis: } \beta_3 > 0.
• The remaining variables capture rates of return. It is not enough simply to add interest rates as a rate of return, and hope for a positive coefficient, because nominal high interest rates in developing countries usually reflect expected inflation, default risk, and devaluation risk.

○ The real interest differential (nominal interest rate on rand government bonds, minus expected inflation, minus the same for abroad) should have a positive effect on the perceived rate of return to holding rand assets and therefore on the value of the rand. Initially we used the one-year lag in the inflation rate as a simple way of capturing expected inflation. We now use better forward-looking measures of expected inflation, in the form of professional forecasts in South Africa and the US: We are now using measures of ex ante expectations: the Federal Reserve Bank of Philadelphia Survey of Professional Forecasters in the case of US inflation and formal Bureau of Economic Research forecasts in the case of South Africa. Hypothesis: \( \beta_4 > 0 \).

A country risk premium is included to control for risk of default, or risk of future imposition of capital controls, when looking for a positive coefficient on the real interest differential. After all, a high interest differential does not attract investors to the extent that it merely reflects a correspondingly high fear of default. The preferred measure of the country risk premium is the spread between the interest rate at which South Africa borrows when borrowing in dollars (not rand, because we want to separate out currency risk) and a foreign dollar interest rate of the same maturity. We have obtained data from the Treasury on the sovereign spread for borrowing by the South African government in dollars. The series is illustrated in Fig. 5. One can see an impressive downward trend in the perceived risk of South African debt since 2002, to well below 100 basis points in early 2006, in tandem with some upgrades of South African debt by rating agencies. Sovereign spreads have come down across emerging markets, of course, but international investors appear to have far more confidence in South Africa than in others, as Fig. 6 shows. Hypothesis: \( \beta_5 < 0 \).

• One possible rationale for including the trend term is the growing role of AIDS. Kaufmann and Weerapana (2005) find statistical evidence that the rand reacts adversely to news about AIDS in South Africa. They attribute the strength of the effect to unpredictability regarding long-term business prospects.

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3 Ang, Bekaert and Wei (2005) provide support for using such survey data.
4 In earlier results we used a proxy: the spread between the corporate rand interest rate and the government rand rate, under the theory that when default risk raises the South African government interest rates, it raises the corporate interest rate proportionately more. But the sovereign spread is a much better measure of country risk.
5 However, we have tried entering a measure of reported AIDS infections directly into the equation and we found no effect. This may be due to the inadequacy of the AIDS measure.
Figure 5. Spreads on South African Dollar Debt

Figure 6. South African spread compared to aggregate of emerging market bonds.

Further details on data sources and how these variables were computed are given in the appendix.  

3. RESULTS

The regression results for the nominal and real exchange rate are highly varied. But the real commodity price index does appear generally to have the hypothesized positive sign. The lagged endogenous variable shows up highly significant, suggesting either a momentum/dragging anchor phenomenon, or else the omission of (serially correlated)

6 MacDonald and Ricci (2004), and the updated version in Ricci (2005) have a rather similar list of variables in their equation. Perhaps our main improvements relative to their set are the expected return variables.
determinants. The Breusch-Godfrey LM Test suggests that the use of the lagged endogenous variable does not leave in its wake much grounds for concern about serial correlation.7

Income \textit{per capita} appears with the wrong sign when the regression is run using the real exchange rate for the entire sample period, and significantly so. (These results are reported in Frankel, 2007.) The same is true when we include total income rather than \textit{per capita}, as in old models based on the demand for money. If we include income \textit{per capita} (or income) without the real mineral price index, then it appears statistically significant and of the expected sign. The explanation is the collinearity of real income with mineral prices. But mineral prices knock out real income when they compete side-by-side. Perhaps when we control for the exogenous supply-side influence of the world mineral prices, the remaining variation in income captures endogenous response to fluctuations in demand, which have negative effects on the trade balance and through this route on the value of the currency. In any case, the results are a decisive rejection of the importance of the Balassa-Samuelson effect in this context. If one is convinced that this conclusion is right, then one should omit the \textit{per capita} income differential from the equation, which also has the added advantage of allowing the use of monthly data rather than quarterly. This is what we do in the tables reported here.

The results for the rate of return variables are important. For many emerging markets, it is hard to find a positive effect of the interest differential on demand for the currency, presumably because nominal interest rates in practice signal rears of inflation, depreciation, and default, rather than high expected returns. The real interest differential has the hypothesized positive effect, as can be seen in the reported tables. Results that use the dollar spread on South African borrowing to measure the risk premium show a highly significant negative effect on the value of the rand, as hypothesized. Unfortunately, the sovereign spread data are only available starting in 1996; these results are not reported in the tables here.

The mid-1990s saw important structural changes in South Africa, with the transition to democracy,8 the end of foreign sanctions, and the removal of most capital controls in March 1995. The capital account liberalization is probably the most relevant of these changes for the exchange rate equation. There had been a dual exchange rate system that had separated the financial market for rand from the trade account, charging customers a higher rand price for foreign exchange if the purpose was to acquire assets abroad.9 These structural changes provide an argument for starting the sample in 1996. Another reason is that the sovereign spread data are only available since 1996 anyway. But we have also continued to run regressions over the longer sample period (those reported here), in order to maximize the number of observations. The capital liberalization evidently vented pressure for capital outflow, because the coefficient on the dummy variable is negative,7

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7 Other researchers have been concerned about the possibility of a unit root, even though this is not as likely in the real exchange as in the nominal exchange rate. MacDonald and Ricci (2004) used the Johansen cointegration test. Du Plessis (2005) commented that the real exchange rate was weakly exogenous in their results, and argued that they could not claim to have a model in which the real exchange rate adjusts toward a long-term equilibrium. Macdonald and Ricci (2005) responded that adding another six quarters of data solved the problem.

8 Aron and Elbadawi (1999) describe a sequence of capital inflows into South Africa after its democratic elections in 1994, followed by a speculative attack in 1996.

and usually significant statistically. On the theory that the degree of capital mobility may have increased in March 1995, we allowed for the possibility of a shift in the coefficient on the real interest differential;\(^{10}\) but the variable (the differential interacted with a dummy that takes the value of 1 post-March 1995) was not statistically significant, or even greater than zero. We also tried estimating the post-1995 sample by itself, but the results were unsatisfactory, perhaps because of the smaller number of observations. Better to go back to the 1980s, even though it means losing the country risk variable.

### Real Exchange Rate based on CPI

**Dependent Variable:** Log(Real Rand \(_{CPI}\))

**Sample(adjusted):** 1984:II-2007:I

**Included observations:** 92 after adjusting endpoints

<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficient</th>
<th>Std. Error</th>
<th>t-Statistic</th>
<th>Prob.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Log(Real Rand (_{CPI}) (-1))</td>
<td>0.839</td>
<td>0.043</td>
<td>19.687</td>
<td>0.0000</td>
</tr>
<tr>
<td>Log(Real World Mineral Price Index)</td>
<td>0.164</td>
<td>0.058</td>
<td>2.816</td>
<td>0.006</td>
</tr>
<tr>
<td>Real Interest Differential</td>
<td>0.018</td>
<td>0.005</td>
<td>3.390</td>
<td>0.0011</td>
</tr>
<tr>
<td>Cap Lib Dummy</td>
<td>-0.050</td>
<td>0.023</td>
<td>-2.154</td>
<td>0.0341</td>
</tr>
<tr>
<td>Cap Lib Dummy * RID</td>
<td>-0.009</td>
<td>0.006</td>
<td>-1.468</td>
<td>0.1457</td>
</tr>
<tr>
<td>C</td>
<td>0.738</td>
<td>0.202</td>
<td>3.652</td>
<td>0.0004</td>
</tr>
</tbody>
</table>

**R-squared** 0.912  
**Adjusted R-squared** 0.907  
**S.E. of regression** 0.065  
**F-statistic** 178.628  
**Sum squared resid** 0.363  
**Prob(F-statistic)** 0.000  
**Log likelihood** 124.047  
**Durbin-Watson stat** 1.718

**Breusch-Godfrey Serial Correlation LM Test:**

- **F-statistic** 0.990  
- **Probability** 0.3759

### Real Exchange Rate based on PPI

**Dependent Variable:** Log(Real Rand \(_{PPI}\))

**Sample(adjusted):** 1984:II- 2007:I

**Included observations:** 92 after adjusting endpoints

<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficient</th>
<th>Std. Error</th>
<th>t-Statistic</th>
<th>Prob.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Log(Real Rand (_{PPI}) (-1))</td>
<td>0.829</td>
<td>0.047</td>
<td>17.716</td>
<td>0.0000</td>
</tr>
<tr>
<td>Log(Real World Mineral Price Index)</td>
<td>0.129</td>
<td>0.054</td>
<td>2.360</td>
<td>0.0206</td>
</tr>
<tr>
<td>Real Interest Differential</td>
<td>0.016</td>
<td>0.005</td>
<td>3.098</td>
<td>0.0026</td>
</tr>
</tbody>
</table>

\(^{10}\) Chinn (1999) found more support for the overshooting version of the monetary model -- where interest rates strengthen the currency -- toward the end of his 1980-1997 sample period, consistent with the 1995 unification of the financial and commercial exchange rates. Akinboade and Makina (2006) test for multiple structural breaks.
### Real Exchange Rate based on GDP Deflator

Dependent Variable: \( \log(\text{Real Rand GDP deflator}) \)
Included observations: 92 after adjusting endpoints

<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficient</th>
<th>Std. Error</th>
<th>t-Statistic</th>
<th>Prob.</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \log(\text{Real Rand} _\text{CPI} (-1)) )</td>
<td>0.847</td>
<td>0.043</td>
<td>19.555</td>
<td>0.0000</td>
</tr>
<tr>
<td>( \log(\text{Real World Mineral Price Index}) )</td>
<td>0.137</td>
<td>0.056</td>
<td>2.461</td>
<td>0.0158</td>
</tr>
<tr>
<td>Real Interest Differential</td>
<td>0.020</td>
<td>0.005</td>
<td>3.629</td>
<td>0.0005</td>
</tr>
<tr>
<td>Cap Lib Dummy</td>
<td>-0.006</td>
<td>0.020</td>
<td>-0.301</td>
<td>0.7644</td>
</tr>
<tr>
<td>Cap Lib Dummy * RID</td>
<td>-0.016</td>
<td>0.006</td>
<td>-2.537</td>
<td>0.0130</td>
</tr>
<tr>
<td>( \text{C} )</td>
<td>0.687</td>
<td>0.199</td>
<td>3.455</td>
<td>0.0009</td>
</tr>
</tbody>
</table>

R-squared 0.890  Mean dependent var 4.731
Adjusted R-squared 0.884  S.D. dependent var 0.185
S.E. of regression 0.063  Sum squared resid 0.341
Log likelihood 126.929  F-statistic 139.849
Durbin-Watson stat 1.707  Prob(F-statistic) 0.000

Breusch-Godfrey Serial Correlation LM Test:
F-statistic 1.082  Probability 0.3434
Obs*R-squared 2.311  Probability 0.3148

4. COMPARING THE EQUATION PREDICTION AND ACTUAL EXCHANGE RATE

Fig. 7, 8, and 9 plot the actual real value of the rand (using different price indices) against the value predicted by the equation. In general the fit is remarkably close.

It is natural to suspect that this may be largely due to the lagged endogenous variable, in which case the equation would not be of much use in forecasting. Fig. 10 adds a “dynamic simulation,” that is, a projected path for the last three years of the sample based only on fundamentals. The value of QIV, 2003, is the last one to use the actual exchange rate for the lagged endogenous variable. From then on, the lagged prediction of the equation itself is used as the lagged endogenous variable, rather than the actual. Nevertheless, based on fundamentals such as a rising price of minerals, the projection
predicts as strong a real appreciation of the rand through mid-2006 as did the fitted values of the regression.

Thus the equation does not supply evidence in favor of the proposition that the rand was overvalued (as of early 2007) when judged by its own past relationship to economic fundamentals. But then efficiency in the financial market sense is not the same thing as efficiency in the sense of correct signals for the allocation of resources in the real economy. \(^{11}\) The speculative inflows during the recent boom in commodities and emerging markets may be “par for the course;” but this is not inconsistent with the proposition that Dutch Disease crowding out of non-commodity tradables could have negative consequences, especially in the long run.

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Figure 7. Actual vs Fitted Real Value of the Rand, based on the CPI (1984:II-2007:I)

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\(^{11}\) Recent theoretical illustrations include Devereux and Engel (2006) and Caballero (2007).
Figure 8. Actual vs Fitted Real Value of the Rand, based on PPI (1984:II-2007:I)

Figure 9. Actual vs Fitted Real Value of the Rand, based on GDP Deflator (1984:II-2007:I)
Figure 10. Actual vs. Fitted vs. Projected Real Value of Rand, based on CPI (1984:II-2007:I)

DATA NOTES

Nominal Exchange Rate (NER): is the nominal foreign exchange value of South Africa’s currency expressed in USD per South African Rand.

Real Bilateral Exchange Rate Index: is the nominal exchange rate multiplied by the ratio of South African price index to US price index, expressed in index form with base year 2000. Three real exchange rate indices are constructed based on three different price indices: Real Rand CPI is calculated using the CPI, Real Rand PPI is calculated using the PPI, and Real Rand GDP deflator is calculated using the GDP deflator. The three series are plotted below for comparison.

Real Mineral and Metal Price Index:
The nominal weighted mineral and metal price index (World Mineral Price Index) is the weighted price index of South African major mineral and metal export commodities. Weights are derived
from the commodity’s export share in the value of total exports of South Africa. While efforts are made to include all major commodities, some of them, such as diamond, are not included due to lack of international price index. The commodities included and their weights are given below:

**Table. South African Major Export Commodities**

<table>
<thead>
<tr>
<th>Commodity Group</th>
<th>Actual % share</th>
<th>Adjusted % share</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gold and platinum</td>
<td>17.54</td>
<td>56.22</td>
</tr>
<tr>
<td>Iron ores</td>
<td>2.78</td>
<td>8.90</td>
</tr>
<tr>
<td>Coal</td>
<td>5.69</td>
<td>18.23</td>
</tr>
<tr>
<td>Petroleum Oil</td>
<td>2.81</td>
<td>9.01</td>
</tr>
<tr>
<td>Aluminum</td>
<td>2.38</td>
<td>7.64</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>31.19</strong></td>
<td><strong>100.00</strong></td>
</tr>
</tbody>
</table>

*Source: Compiled from data from South African Trade and Industry Department*

The real weighted mineral and metal price index (Real World Mineral Price Index) is the World Mineral Price Index divided by the consumer price index of the US.

*Expected Inflation Rates:* The source of US’s expected inflation rate is the Federal Reserve Bank of Philadelphia. The South Africa expected inflation rate is the inflation forecasts from the macro model of South Africa’s Bureau of Economic Research, provided by Professor Ben W Smit.

*Real Interest Rate Differentials:* The long term government bond yields of the US and South Africa are obtained from the IFS, IMF database. Then respective expected inflations are subtracted from nominal long term bond yields to get the real interest rates. The real interest rate differential is then the difference between SA’s real government bond rate and US’s real government bond rate.

*GDP Ratios*

Real and nominal GDPs are collected for South Africa and the US from IFS, IMF, and the following ratio are calculated:

(i) Real GDP ratio between S. Africa and the US (RGDPrat)

(ii) Nominal GDP ratio between S. Africa and the US (NGDPrat)

(iii) Real per capita GDP ratio between S. Africa and the US (PERGDPPrat)

Quarterly *per capita* GDPs are calculated using quarterly real GDPs and extrapolated quarterly population. The annual mid-year population estimates, obtained from IFS, were decomposed to quarterly using the following formula:

\[
\text{Year } t \ Q1 \ pop = \frac{3}{8} \times (\text{year } t-1 \ pop) + \frac{5}{8} \times (\text{year } t \ pop) \\
Q2 \ pop = \frac{1}{8} \times (\text{year } t-1 \ pop) + \frac{7}{8} \times (\text{year } t \ pop) \\
Q3 \ pop = \frac{7}{8} \times (\text{year } t \ pop) + \frac{1}{8} \times (\text{year } t+1 \ pop) \\
Q4 \ pop = \frac{5}{8} \times (\text{year } t \ pop) + \frac{3}{8} \times (\text{year } t+1 \ pop)
\]

The following Fig. show how the generated quarterly *per capita* GDP series tracked the annual figures obtained from the World Development Indicators, World Bank.

*Figure. Annual (top) and Quarterly (bottom) series of per capita GDP: South Africa*
Figure. Annual (top) and Quarterly (bottom) series of per capita GDP: USA
Dummy for Removal of Capital Controls (Cap Lib Dummy): A dummy for capital market liberalization, which has a value of one since the second quarter of 1995, when South African capital market was liberalized, and zero elsewhere. Cap Lib Dummy * RID comes from Cap Lib Dummy interacted with the real interest rate differential.

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